



Lesson 34: Review of the Assumptions

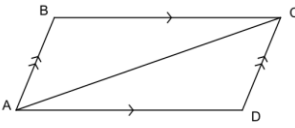
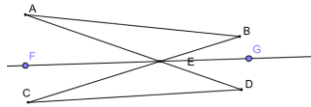
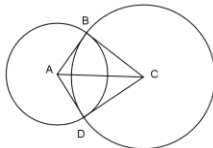
Student Outcomes

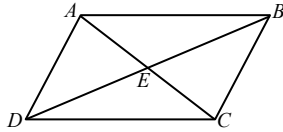
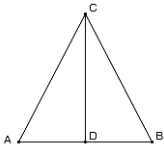
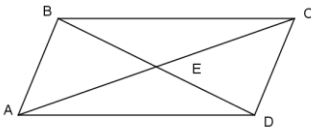
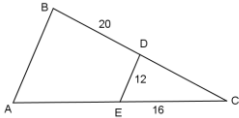
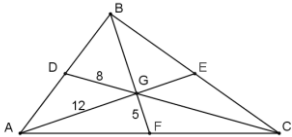
- Students review the principles addressed in Module 1.

Lesson Notes

In Lesson 33, we reviewed many of the assumptions, facts, and properties used in this module to derive other facts and properties in geometry. We continue this review process with the table of facts and properties below, beginning with those related to rigid motions.

Classwork (40 minutes)

Assumption/Fact/Property	Guiding Questions/Applications	Notes/Solutions
<p>Given two triangles $\triangle ABC$ and $\triangle A'B'C'$ so that $AB = A'B'$ (Side), $m\angle A = m\angle A'$ (Angle), $AC = A'C'$ (Side), then the triangles are congruent. [SAS]</p>	<p>The figure below is a parallelogram ABCD. What parts of the parallelogram satisfy the SAS triangle congruence criteria for $\triangle ABD$ and $\triangle CDB$? Describe a rigid motion(s) that will map one onto the other.</p> 	<p>$AD = CB$, Property of a parallelogram $m\angle ABD = m\angle CDB$, Alternate interior angles $BD = BD$, Reflexive property $\triangle ABD \cong \triangle CDB$, SAS 180° Rotation about the midpoint of BD</p>
<p>Given two triangles $\triangle ABC$ and $\triangle A'B'C'$, if $m\angle A = m\angle A'$ (Angle), $AB = A'B'$ (Side), and $m\angle B = m\angle B'$ (Angle), then the triangles are congruent. [ASA]</p>	<p>In the figure below, $\triangle CDE$ is the image of reflection of $\triangle ABE$ across line FG. Which parts of the triangle can be used to satisfy the ASA congruence criteria?</p> 	<p>$m\angle AEB = m\angle CED$, Vertical angles are equal in measure. $BE = DE$, Reflections map segments onto segments of equal length $\angle B \cong \angle D$, Reflections map angles onto angles of equal measure.</p>
<p>Given two triangles $\triangle ABC$ and $\triangle A'B'C'$, if $AB = A'B'$ (Side), $AC = A'C'$ (Side), and $BC = B'C'$ (Side), then the triangles are congruent. [SSS]</p>	<p>$\triangle ABC$ and $\triangle ADC$ are formed from the intersections and center points of circles A and C. Prove $\triangle ABC \cong \triangle ADC$ by SSS.</p> 	<p>AC is a common side, $AB = AD$; they are both radii of the same circle. $BC = DC$, they are both radii of the same circle. Thus, $\triangle ABC \cong \triangle ADC$ by SSS.</p>

<p>Given two triangles $\triangle ABC$ and $\triangle A'B'C'$, if $AB = A'B'$ (Side), $m\angle B = m\angle B'$ (Angle), and $\angle C = \angle C'$ (Angle), then the triangles are congruent. [SAA]</p>	<p>The AAS congruence criterion is essentially the same as the ASA criterion for proving triangles congruent. Why is this true?</p> 	<p>If two angles of a triangle are congruent to two angles of a second triangle, then the third pair must also be congruent. Therefore, if one pair of corresponding sides is congruent, we treat the given corresponding sides as the included side and the triangles are congruent by ASA.</p>
<p>Given two right triangles ABC and $A'B'C'$ with right angles $\angle B$ and $\angle B'$, if $AB = A'B'$ (Leg) and $AC = A'C'$ (Hypotenuse), then the triangles are congruent. [HL]</p>	<p>In the figure below, CD is the perpendicular bisector of AB and $\triangle ABC$ is isosceles. Name the two congruent triangles appropriately and describe the necessary steps for proving them congruent using HL.</p> 	<p>$\triangle ADC \cong \triangle BDC$ Given $CD \perp AB$, both $\triangle ADC$ and $\triangle BDC$ are right triangles. CD is a common side. Given $\triangle ABC$ is isosceles, $\overline{AC} \cong \overline{CB}$.</p>
<p>The opposite sides of a parallelogram are congruent.</p> <p>The opposite angles of a parallelogram are congruent.</p> <p>The diagonals of a parallelogram bisect each other.</p>	<p>In the figure below, $BE \cong DE$ and $\angle CBE \cong \angle ADE$. Prove $ABCD$ is a parallelogram.</p> 	<p>$\angle BEC \cong \angle AED$, vertical angles are equal in measure $\overline{BE} \cong \overline{DE}$ and $\angle CBE \cong \angle ADE$, given. $\triangle BEC \cong \triangle DEA$, ASA. By similar reasoning, we can show that $\triangle BEA \cong \triangle DEC$. Since $\overline{AB} \cong \overline{DC}$ and $\overline{BC} \cong \overline{DA}$, $ABCD$ is a parallelogram because the opposite sides are congruent (property of -ogram).</p>
<p>The mid-segment of a triangle is a line segment that connects the midpoints of two sides of a triangle; the mid-segment is parallel to the third side of the triangle and is half the length of the third side.</p>	<p>DE is the mid-segment of $\triangle ABC$. Find the perimeter of $\triangle ABC$, given the labeled segment lengths.</p> 	<p>96</p>
<p>The three medians of a triangle are concurrent at the centroid; the centroid divides each median into two parts, from vertex to centroid and centroid to midpoint in a ratio of 2:1.</p>	<p>If \overline{AE}, \overline{BF}, and \overline{CD} are medians of $\triangle ABC$, find the lengths of segments BG, GE, and CG, given the labeled lengths.</p> 	<p>$BG = 10$ $GE = 6$ $CG = 16$</p>

Exit Ticket (5 minutes)

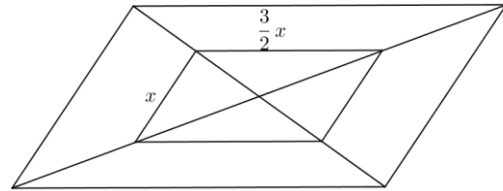
Name _____

Date _____

Lesson 34: Review of the Assumptions

Exit Ticket

The inner parallelogram in the figure is formed from the midsegments of the four triangles created by the outer parallelogram's diagonals. The lengths of the smaller and larger midsegments are as indicated. If the perimeter of the outer parallelogram is 40, find the value of x .



Exit Ticket Sample Solutions

The following solutions indicate an understanding of the objectives of this lesson:

The inner parallelogram in the figure is formed from the midsegments of the four triangles created by the outer parallelogram's diagonals. The lengths of the smaller and larger midsegments are as indicated. If the perimeter of the outer parallelogram is 40, find the value of x .

$x = 4$

Problem Set Sample Solutions

The following solutions indicate an understanding of the objectives of this lesson:

Use any of the assumptions, facts, and/or properties presented in the tables above to find x and/or y in each figure below. Justify your solutions.

- Find the perimeter of parallelogram $ABCD$. Justify your solution.
 $100, 15 = x + 4, x = 11$
- $AC = 34$
 $AB = 26$
 $BD = 28$
 Find the perimeter of $\triangle CED$. Justify your solution.
 57
 $CE = \frac{1}{2}AC; CE = 17$
 $CD = AB; CE = 26$
 $ED = \frac{1}{2}BD; ED = 14$
 $Perimeter = 17 + 26 + 14 = 57$
- $XY = 12$
 $XZ = 20$
 $ZY = 24$
 $F, G,$ and H are midpoints of the sides on which they are located. Find the perimeter of $\triangle FGH$. Justify your solution.
 $28.$ The midsegment is half the length of the side of the triangle it is parallel to.

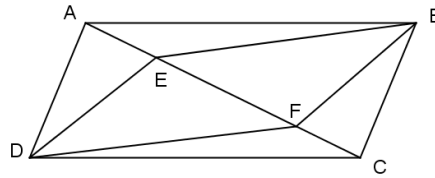
4. $ABCD$ is a parallelogram with $AE = CF$.
Prove that $DEBF$ is a parallelogram.

$AE = CF$
 $AD = BC$
 $m\angle DAE = m\angle BCF$

$\triangle ADE \cong \triangle CBF$
 $DE = BF$
 $AB = DC$
 $m\angle BAE = m\angle DCF$

$\triangle BAE \cong \triangle DCF$
 $BE = DF$
 $\therefore ABCD$ is a parallelogram

Given
Property of a parallelogram
If parallel lines are cut by a transversal, then alternate interior angles are equal in measure
SAS
Corresponding sides of congruent triangles are congruent
Property of a parallelogram
If parallel lines are cut by a transversal, then alternate interior angles are equal in measure
SAS
Corresponding sides of congruent triangles are congruent
If both sets of opp. sides of a quad. are equal in length, then the quad. is a parallelogram.



5. C is the centroid of $\triangle RST$.
 $RC = 16$, $CL = 10$, $TJ = 21$

$SC = \underline{20}$
 $TC = \underline{14}$
 $KC = \underline{8}$

