



Lesson 1: The Area of Parallelograms Through Rectangle

Facts

Student Outcomes

- Students show the area formula for the region bounded by a parallelogram by composing it into rectangles. They understand that the area of a parallelogram is the area of the region bounded by the parallelogram.

Lesson Notes

For students to participate in the discussions, each will need the parallelogram templates attached to this lesson, along with the following: scissors, glue, ruler, and paper on which to glue their shapes.

Fluency Exercise (5 minutes)

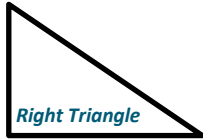
Multiplication of Fractions Sprint

Classwork


Opening Exercise (4 minutes)

Students name the given shapes.

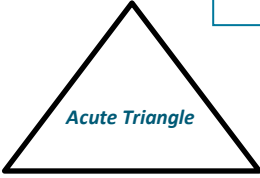
Opening Exercise
Name each shape.




Right Triangle




Parallelogram



Acute Triangle



Rectangle



Trapezoid

Scaffolding:

Some students may not know this vocabulary yet, so creating a poster or chart for student desks may help them to remember these terms.

- Identify the shape that is commonly referred to as a parallelogram. How do you know it's a parallelogram?

NOTE: A rectangle is considered a parallelogram, but is commonly called a rectangle because it is a more specific name.

- The shape is a quadrilateral (4-sided) and has two sets of parallel lines.*

- What are some quadrilaterals that you know?
 - *Answers will vary.*
- Today we are going to find the area of one of these quadrilaterals: the parallelogram. We are going to use our knowledge of the area of rectangles to help us. Who can remind us what we mean by area?
 - *The number of square units that make up the inside of the shape.*

NOTE: Students with limited English would benefit from a further discussion of area that relates to things they have personal connections to.

- Talk to your neighbor about how to calculate area of a rectangle.

Once students have had time for discussion, teachers should pick someone who can clearly explain how to find the area of a rectangle.

- *Count the number of square units inside the shape (if that is given) or multiply the base by the height.*

Discussion (10 minutes)

Provide each student with the picture of a parallelogram provided as an attachment to this lesson.

- What shape do you have in front of you?
 - *A parallelogram.*
- Work with a partner to make a prediction of how we would calculate the area of the shape.
 - *Answers will vary.*
- Cut out the parallelogram.
- Since we know how to find the area of a rectangle, how can we change the parallelogram into a rectangle?
 - *Cut off a triangle on one side of the parallelogram and glue it to the other side.*
- Draw a dotted perpendicular line to show the triangle you will cut. Fold your paper along this line.



Check to make sure all students have drawn the dotted line in the correct place before instructing them to cut. Explain that the fold on the line shows that the two right angles form a 180° angle.

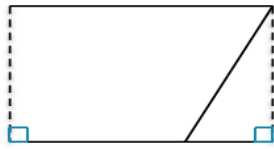
- Could the dotted line be drawn in a different location? If so, where?
 - *The dotted line can be drawn in a different location. It could be drawn on the other side of the parallelogram, displayed below.*



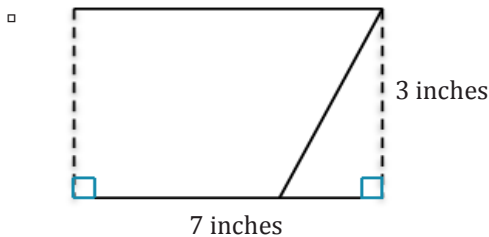
- The base and height of a parallelogram form a right angle.

MP.7

- Measure (inches) the base and height of the parallelogram using the correct mathematical tools.
 - *The base is 7 inches, and the height is 3 inches.*
- Cut along the dotted line.
- Glue both parts of the parallelogram onto a piece of paper to make a rectangle.



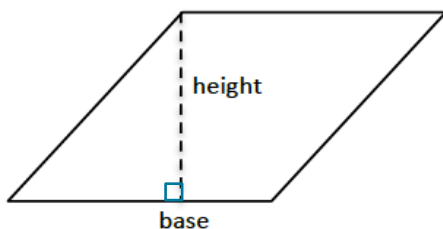
- What shape did you create?
 - *A rectangle.*
- Use the correct mathematical tool to measure (inches) and label each side of the rectangle created from the original parallelogram.



- How does this compare to the base and height of the parallelogram?
 - *They are the same.*
- When we moved the triangle, did the area inside the shape change? Explain.
 - *The area did not change because it is the same size. It just looks different.*
- What is the area of the rectangle?
 - *21 square inches or 21 inches squared or 21 in².*

NOTE: English learners would benefit from a discussion on why all three of these answers represent the same value.

- If the area of the rectangle is 21 square inches, what is the area of the original parallelogram? Why?
 - *The area of the original parallelogram is also 21 square inches because both shapes have the same amount of space inside.*
- We know the formula for the area of a rectangle is $Area = base \times height$, or $A = bh$. What is the formula to calculate the area of a parallelogram?
 - *The formula to calculate the area of a parallelogram would be the same as a rectangle, $A = bh$.*
- Examine the given parallelogram, label the base and height.



MP.7

MP.7

- Why is the height the vertical line and not the slanted edge?

NOTE: English learners may need a further explanation of the meaning of the slanted edge.

- If we look back to the rectangle we created, the base and height of both the rectangle and the original parallelogram are perpendicular to each other. Therefore, the height of a parallelogram is the perpendicular line drawn from the top base to the bottom base.

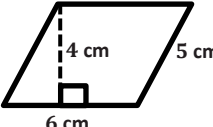
Exercise 1 (5 minutes)

Students work individually to complete the following problems.

Exercises

1. Find the area of each parallelogram below. Each figure is not drawn to scale.

a.



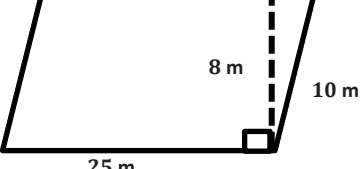
6 cm

$$A = bh$$

$$= 6 \text{ cm}(4 \text{ cm})$$

$$= 24 \text{ cm}^2$$

b.



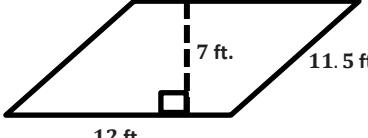
25 m

$$A = bh$$

$$= 25 \text{ m}(8 \text{ m})$$

$$= 200 \text{ m}^2$$

c.



12 ft.

$$A = bh$$

$$= 12 \text{ ft.}(7 \text{ ft.})$$

$$= 84 \text{ ft.}^2$$

Scaffolding:
English learners may need some clarification about what it means to not be drawn to scale and why this may be the case.

Discussion (8 minutes)

- How could we construct a rectangle from this parallelogram?
 - Students will try to draw the height of the parallelogram differently.
- Why can't we use the same method we used previously?
 - The vertical dotted line does not go through the entire parallelogram.



Students will struggle drawing the height because they will not be sure whether part of the height can be outside of the parallelogram.

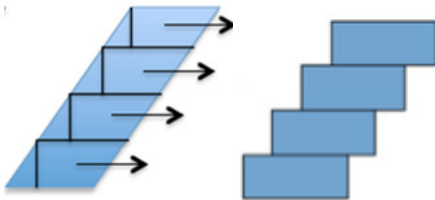
- Cut out the shape.
- To solve this problem, we are actually going to cut the parallelogram horizontally into four equal pieces. Use the appropriate measurement tool to determine where to make the cuts.

Allow time for students to think about how to approach this problem. If time allows, have students share their thoughts before the teacher demonstrates how to move forward.

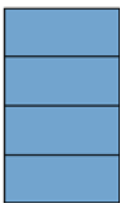
Teacher should demonstrate these cuts before allowing students to make the cuts.



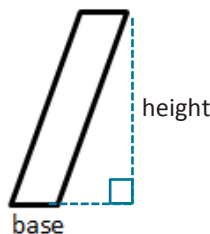
- We have four parallelograms. How can we use them to calculate the area of the parallelogram?
 - Turn each of the parallelograms into rectangles.
- How can we make these parallelograms into rectangles?
 - Cut a right triangle off of every parallelogram and move the right triangle to the other side of the parallelogram.



- How can we show that the original parallelogram forms a rectangle?
 - If we push all the rectangles together, they will form one rectangle.



- Therefore, it does not matter how tilted a parallelogram is. The formula to calculate the area will always be the same as the area formula of a rectangle.
- Draw and label the height of the parallelogram below.

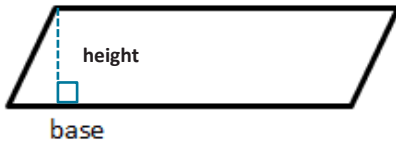
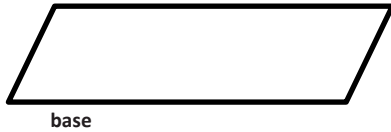


Exercise 2 (5 minutes)

Students complete the exercises individually.

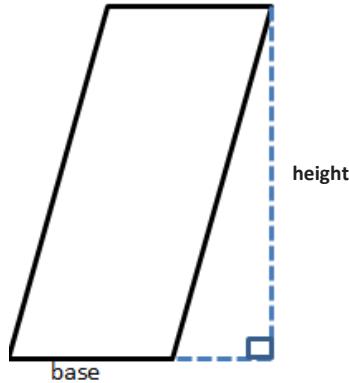
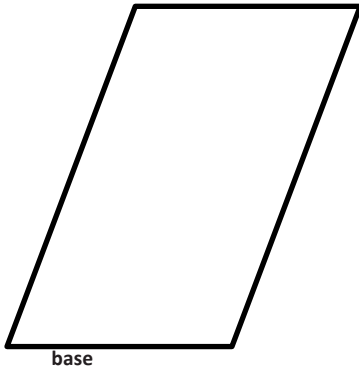
2. Draw and label the height of each parallelogram. Use the correct mathematical tool to measure (in inches) the base and height, and calculate the area of each parallelogram.

a.



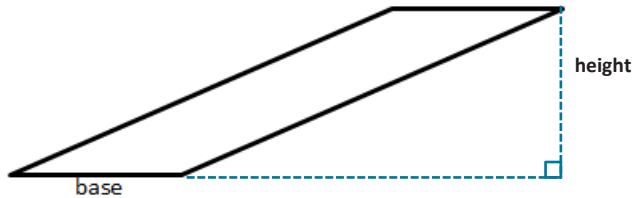
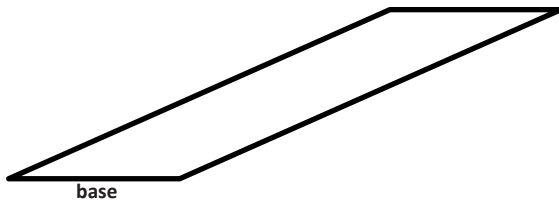
$$A = bh = (0.5 \text{ in.})(2 \text{ in.}) = 1 \text{ in}^2$$

b.



$$A = bh = (1.5 \text{ in.})(2 \text{ in.}) = 3 \text{ in}^2$$

c.



$$A = bh = (1 \text{ in.})(1 \text{ in.}) = 1 \text{ in}^2$$

3. If the area of a parallelogram is $\frac{35}{42} \text{ cm}^2$ and the height is $\frac{1}{7} \text{ cm}$, write an equation that relates the height, base, and area of the parallelogram. Solve the equation.

$$\begin{aligned}\frac{35}{42} \text{ cm}^2 &= b\left(\frac{1}{7} \text{ cm}\right) \\ \frac{35}{42} \text{ cm}^2 \div \frac{1}{7} \text{ cm} &= b\left(\frac{1}{7} \text{ cm}\right) \div \frac{1}{7} \text{ cm} \\ \frac{35}{6} \text{ cm} &= b \\ 5\frac{5}{6} \text{ cm} &= b\end{aligned}$$

Scaffolding:

English learners may benefit from a sentence starter, such as “The formulas are the same because ...”

Closing (3 minutes)

- Why are the area formulas for rectangles and parallelograms the same?

Lesson Summary

The formula to calculate the area of a parallelogram is $A = bh$, where b represents the base and h represents the height of the parallelogram.

The height of a parallelogram is the line segment perpendicular to the base. The height is drawn from a vertex that is opposite the base.

Exit Ticket (5 minutes)

Name _____

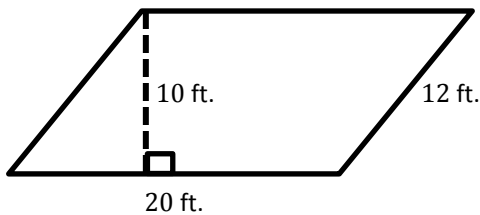
Date _____

Lesson 1: The Area of Parallelograms Through Rectangle Facts

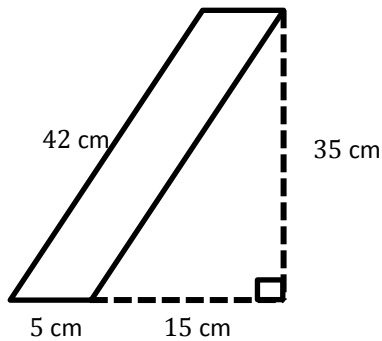
Exit Ticket

Calculate the area of each parallelogram. The figures are not drawn to scale.

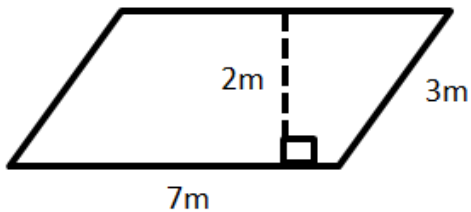
1.



2.



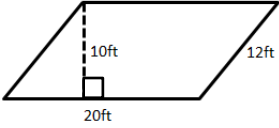
3.



Exit Ticket Sample Solutions

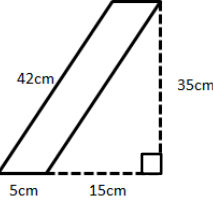
Calculate the area of each parallelogram. The figures are not drawn to scale.

1.



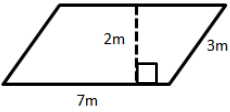
$A = bh = 20 \text{ ft.} (10 \text{ ft.}) = 200 \text{ ft}^2$

2.



$A = bh = 5 \text{ cm} (35 \text{ cm}) = 175 \text{ cm}^2$

3.




$A = bh = 7 \text{ m} (2 \text{ m}) = 14 \text{ m}^2$

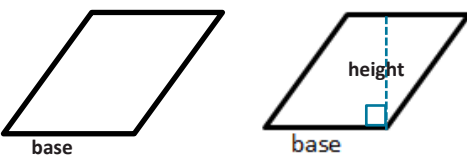
Problem Set Sample Solutions

Draw and label the height of each parallelogram.

1.

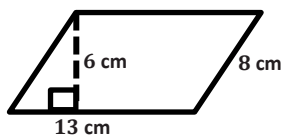


2.



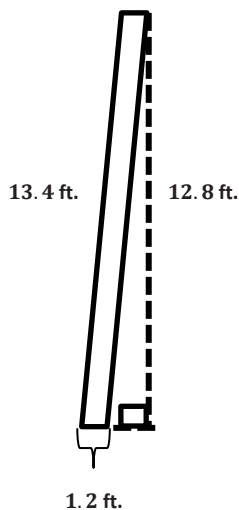
Calculate the area of each parallelogram. The figures are not drawn to scale.

3.



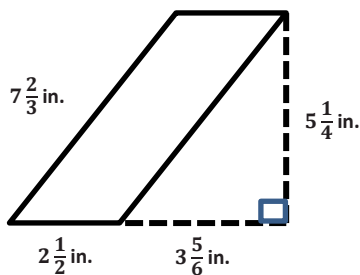
$$\begin{aligned} A &= bh \\ &= 13 \text{ cm}(6 \text{ cm}) \\ &= 78 \text{ cm}^2 \end{aligned}$$

4.



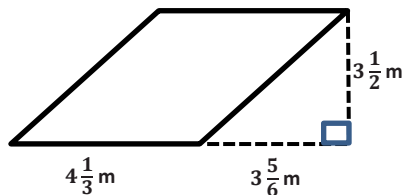
$$\begin{aligned} A &= bh \\ &= 1.2 \text{ ft.}(12.8 \text{ ft.}) \\ &= 15.36 \text{ ft}^2 \end{aligned}$$

5.



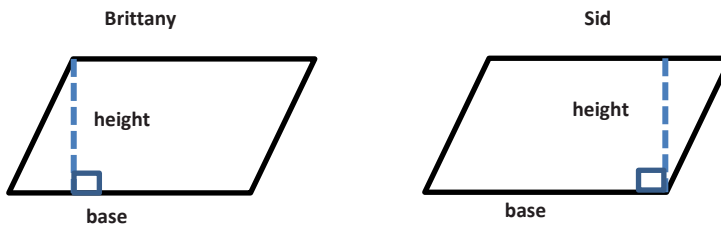
$$\begin{aligned} A &= bh \\ &= 2\frac{1}{2} \text{ in.} \left(5\frac{1}{4} \text{ in.}\right) \\ &= \frac{5}{2} \text{ in.} \left(\frac{21}{4} \text{ in.}\right) \\ &= \frac{105}{8} \text{ in}^2 \\ &= 13\frac{1}{8} \text{ in}^2 \end{aligned}$$

6.



$$\begin{aligned} A &= bh \\ &= 4\frac{1}{3} \text{ m} \left(3\frac{1}{2} \text{ m}\right) \\ &= \frac{13}{3} \text{ m} \left(\frac{7}{2} \text{ m}\right) \\ &= \frac{91}{6} \text{ m}^2 \\ &= 15\frac{1}{6} \text{ m}^2 \end{aligned}$$

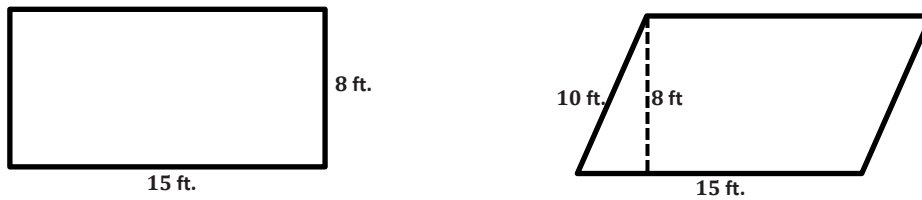
7. Brittany and Sid were both asked to draw the height of a parallelogram. Their answers are below.



Are both Brittany and Sid correct? If not, who is correct? Explain your answer.

Both Brittany and Sid are correct because both of their heights represent a line segment that is perpendicular to the base and whose endpoint is the opposite side of the parallelogram.

8. Do the rectangle and parallelogram below have the same area? Explain why or why not.



Yes, the rectangle and parallelogram have the same area because if we cut off the triangle on the left side of the parallelogram, we can move it over to the right and make the parallelogram into a rectangle. At this time, both rectangles would have the same dimensions; therefore, their areas would be the same.

9. A parallelogram has an area of 20.3 sq. cm and a base of 2.5 cm. Write an equation that relates the area to the base and height, h . Solve the equation to determine the length of the height.

$$20.3 \text{ cm}^2 = 2.5 \text{ cm}(h)$$

$$20.3 \text{ cm}^2 \div 2.5 \text{ cm} = 2.5 \text{ cm}(h) \div 2.5 \text{ cm}$$

$$8.12 \text{ cm} = h$$

Multiplication of Fractions – Round 1

Directions: *Determine the product of the fractions.*

Number Correct: _____

1.	$\frac{1}{2} \times \frac{3}{4}$	
2.	$\frac{5}{6} \times \frac{5}{7}$	
3.	$\frac{3}{4} \times \frac{7}{8}$	
4.	$\frac{4}{5} \times \frac{8}{9}$	
5.	$\frac{1}{4} \times \frac{3}{7}$	
6.	$\frac{5}{7} \times \frac{4}{9}$	
7.	$\frac{3}{5} \times \frac{1}{8}$	
8.	$\frac{2}{9} \times \frac{7}{9}$	
9.	$\frac{1}{3} \times \frac{2}{5}$	
10.	$\frac{3}{7} \times \frac{5}{8}$	
11.	$\frac{2}{3} \times \frac{9}{10}$	
12.	$\frac{3}{5} \times \frac{1}{6}$	
13.	$\frac{2}{7} \times \frac{3}{4}$	
14.	$\frac{5}{8} \times \frac{3}{10}$	
15.	$\frac{4}{5} \times \frac{7}{8}$	

16.	$\frac{8}{9} \times \frac{3}{4}$	
17.	$\frac{3}{4} \times \frac{4}{7}$	
18.	$\frac{1}{4} \times \frac{8}{9}$	
19.	$\frac{3}{5} \times \frac{10}{11}$	
20.	$\frac{8}{13} \times \frac{7}{24}$	
21.	$2\frac{1}{2} \times 3\frac{3}{4}$	
22.	$1\frac{4}{5} \times 6\frac{1}{3}$	
23.	$8\frac{2}{7} \times 4\frac{5}{6}$	
24.	$5\frac{2}{5} \times 2\frac{1}{8}$	
25.	$4\frac{6}{7} \times 1\frac{1}{4}$	
26.	$2\frac{2}{3} \times 4\frac{2}{5}$	
27.	$6\frac{9}{10} \times 7\frac{1}{3}$	
28.	$1\frac{3}{8} \times 4\frac{2}{5}$	
29.	$3\frac{5}{6} \times 2\frac{4}{15}$	
30.	$4\frac{1}{3} \times 5$	

Multiplication of Fractions – Round 1 [KEY]

Directions: Determine the product of the fractions.

1.	$\frac{1}{2} \times \frac{3}{4}$	$\frac{3}{8}$
2.	$\frac{5}{6} \times \frac{5}{7}$	$\frac{25}{42}$
3.	$\frac{3}{4} \times \frac{7}{8}$	$\frac{21}{32}$
4.	$\frac{4}{5} \times \frac{8}{9}$	$\frac{32}{45}$
5.	$\frac{1}{4} \times \frac{3}{7}$	$\frac{3}{28}$
6.	$\frac{5}{7} \times \frac{4}{9}$	$\frac{20}{63}$
7.	$\frac{3}{5} \times \frac{1}{8}$	$\frac{3}{40}$
8.	$\frac{2}{9} \times \frac{7}{9}$	$\frac{14}{81}$
9.	$\frac{1}{3} \times \frac{2}{5}$	$\frac{2}{15}$
10.	$\frac{3}{7} \times \frac{5}{8}$	$\frac{15}{56}$
11.	$\frac{2}{3} \times \frac{9}{10}$	$\frac{18}{30} = \frac{3}{5}$
12.	$\frac{3}{5} \times \frac{1}{6}$	$\frac{3}{30} = \frac{1}{10}$
13.	$\frac{2}{7} \times \frac{3}{4}$	$\frac{6}{28} = \frac{3}{14}$
14.	$\frac{5}{8} \times \frac{3}{10}$	$\frac{15}{80} = \frac{3}{16}$
15.	$\frac{4}{5} \times \frac{7}{8}$	$\frac{28}{40} = \frac{7}{10}$

16.	$\frac{8}{9} \times \frac{3}{4}$	$\frac{24}{36} = \frac{2}{3}$
17.	$\frac{3}{4} \times \frac{4}{7}$	$\frac{12}{28} = \frac{3}{7}$
18.	$\frac{1}{4} \times \frac{8}{9}$	$\frac{8}{36} = \frac{2}{9}$
19.	$\frac{3}{5} \times \frac{10}{11}$	$\frac{30}{55} = \frac{6}{11}$
20.	$\frac{8}{13} \times \frac{7}{24}$	$\frac{56}{312} = \frac{7}{39}$
21.	$2\frac{1}{2} \times 3\frac{3}{4}$	$\frac{75}{8} = 9\frac{3}{8}$
22.	$1\frac{4}{5} \times 6\frac{1}{3}$	$\frac{171}{15} = 11\frac{2}{5}$
23.	$8\frac{2}{7} \times 4\frac{5}{6}$	$\frac{1682}{42} = 40\frac{1}{21}$
24.	$5\frac{2}{5} \times 2\frac{1}{8}$	$\frac{459}{40} = 11\frac{19}{40}$
25.	$4\frac{6}{7} \times 1\frac{1}{4}$	$\frac{170}{28} = 6\frac{1}{14}$
26.	$2\frac{2}{3} \times 4\frac{2}{5}$	$\frac{176}{15} = 11\frac{11}{15}$
27.	$6\frac{9}{10} \times 7\frac{1}{3}$	$\frac{1518}{30} = 50\frac{3}{5}$
28.	$1\frac{3}{8} \times 4\frac{2}{5}$	$\frac{242}{40} = 6\frac{1}{20}$
29.	$3\frac{5}{6} \times 2\frac{4}{15}$	$\frac{782}{90} = 8\frac{31}{45}$
30.	$4\frac{1}{3} \times 5$	$\frac{65}{3} = 21\frac{2}{3}$



Multiplication of Fractions – Round 2

Number Correct: _____

Directions: *Determine the product of the fractions.*

Improvement: _____

1.	$\frac{5}{6} \times \frac{1}{4}$	
2.	$\frac{2}{3} \times \frac{5}{7}$	
3.	$\frac{1}{3} \times \frac{2}{5}$	
4.	$\frac{5}{7} \times \frac{5}{8}$	
5.	$\frac{3}{8} \times \frac{7}{9}$	
6.	$\frac{3}{4} \times \frac{5}{6}$	
7.	$\frac{2}{7} \times \frac{3}{8}$	
8.	$\frac{1}{4} \times \frac{3}{4}$	
9.	$\frac{5}{8} \times \frac{3}{10}$	
10.	$\frac{6}{11} \times \frac{1}{2}$	
11.	$\frac{6}{7} \times \frac{5}{8}$	
12.	$\frac{1}{6} \times \frac{9}{10}$	
13.	$\frac{3}{4} \times \frac{8}{9}$	
14.	$\frac{5}{6} \times \frac{2}{3}$	
15.	$\frac{1}{4} \times \frac{8}{11}$	

16.	$\frac{3}{7} \times \frac{2}{9}$	
17.	$\frac{4}{5} \times \frac{10}{13}$	
18.	$\frac{2}{9} \times \frac{3}{8}$	
19.	$\frac{1}{8} \times \frac{4}{5}$	
20.	$\frac{3}{7} \times \frac{2}{15}$	
21.	$1\frac{1}{2} \times 4\frac{3}{4}$	
22.	$2\frac{5}{6} \times 3\frac{3}{8}$	
23.	$1\frac{7}{8} \times 5\frac{1}{5}$	
24.	$6\frac{2}{3} \times 2\frac{3}{8}$	
25.	$7\frac{1}{2} \times 3\frac{6}{7}$	
26.	$3 \times 4\frac{1}{3}$	
27.	$2\frac{3}{5} \times 5\frac{1}{6}$	
28.	$4\frac{2}{5} \times 7$	
29.	$1\frac{4}{7} \times 2\frac{1}{2}$	
30.	$3\frac{5}{6} \times \frac{3}{10}$	

Multiplication of Fractions – Round 2 [KEY]

Directions: Determine the product of the fractions.

1.	$\frac{5}{6} \times \frac{1}{4}$	$\frac{5}{24}$
2.	$\frac{2}{3} \times \frac{5}{7}$	$\frac{10}{21}$
3.	$\frac{1}{3} \times \frac{2}{5}$	$\frac{2}{15}$
4.	$\frac{5}{7} \times \frac{5}{8}$	$\frac{25}{56}$
5.	$\frac{3}{8} \times \frac{7}{9}$	$\frac{21}{72} = \frac{7}{24}$
6.	$\frac{3}{4} \times \frac{5}{6}$	$\frac{15}{24} = \frac{5}{8}$
7.	$\frac{2}{7} \times \frac{3}{8}$	$\frac{6}{56} = \frac{3}{28}$
8.	$\frac{1}{4} \times \frac{3}{4}$	$\frac{3}{16}$
9.	$\frac{5}{8} \times \frac{3}{10}$	$\frac{15}{80} = \frac{3}{16}$
10.	$\frac{6}{11} \times \frac{1}{2}$	$\frac{6}{22} = \frac{3}{11}$
11.	$\frac{6}{7} \times \frac{5}{8}$	$\frac{30}{56} = \frac{15}{28}$
12.	$\frac{1}{6} \times \frac{9}{10}$	$\frac{9}{60} = \frac{3}{20}$
13.	$\frac{3}{4} \times \frac{8}{9}$	$\frac{24}{36} = \frac{2}{3}$
14.	$\frac{5}{6} \times \frac{2}{3}$	$\frac{10}{18} = \frac{5}{9}$
15.	$\frac{1}{4} \times \frac{8}{11}$	$\frac{8}{44} = \frac{2}{11}$

16.	$\frac{3}{7} \times \frac{2}{9}$	$\frac{6}{63} = \frac{2}{21}$
17.	$\frac{4}{5} \times \frac{10}{13}$	$\frac{40}{65} = \frac{8}{13}$
18.	$\frac{2}{9} \times \frac{3}{8}$	$\frac{6}{72} = \frac{1}{12}$
19.	$\frac{1}{8} \times \frac{4}{5}$	$\frac{4}{40} = \frac{1}{10}$
20.	$\frac{3}{7} \times \frac{2}{15}$	$\frac{6}{105} = \frac{2}{35}$
21.	$1\frac{1}{2} \times 4\frac{3}{4}$	$\frac{57}{8}$
22.	$2\frac{5}{6} \times 3\frac{3}{8}$	$\frac{459}{48} = 9\frac{9}{16}$
23.	$1\frac{7}{8} \times 5\frac{1}{5}$	$\frac{390}{40} = 9\frac{3}{4}$
24.	$6\frac{2}{3} \times 2\frac{3}{8}$	$\frac{380}{24} = 15\frac{5}{6}$
25.	$7\frac{1}{2} \times 3\frac{6}{7}$	$\frac{405}{14} = 28\frac{13}{14}$
26.	$3 \times 4\frac{1}{3}$	$\frac{39}{3} = 13$
27.	$2\frac{3}{5} \times 5\frac{1}{6}$	$\frac{403}{30} = 13\frac{13}{30}$
28.	$4\frac{2}{5} \times 7$	$\frac{154}{5} = 30\frac{4}{5}$
29.	$1\frac{4}{7} \times 2\frac{1}{2}$	$\frac{55}{14} = 3\frac{13}{14}$
30.	$3\frac{5}{6} \times \frac{3}{10}$	$\frac{69}{60} = 1\frac{3}{20}$