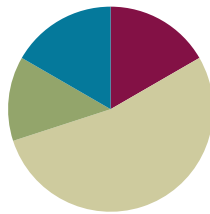


## Lesson 1

**Objective:** Express metric length measurements in terms of a smaller unit; model and solve addition and subtraction word problems involving metric length.

### Suggested Lesson Structure

|                       |                     |
|-----------------------|---------------------|
| ■ Fluency Practice    | (10 minutes)        |
| ■ Application Problem | (8 minutes)         |
| ■ Concept Development | (32 minutes)        |
| ■ Student Debrief     | (10 minutes)        |
| <b>Total Time</b>     | <b>(60 minutes)</b> |



### Fluency Practice (10 minutes)

- Convert Units **4.MD.1** (2 minutes)
- Meter and Centimeter Number Bonds **4.MD.1** (8 minutes)

### Convert Units (2 minutes)

Note: Reviewing these conversions in isolation will help students apply their operations in word problems.

T: (Write  $100\text{ cm} = \underline{\hspace{1cm}}\text{ m}$ .) 100 centimeters is the same as how many meters?

S: 1 meter.

Repeat process using the following possible sequence: 200 cm, 300 cm, 800 cm, and 500 cm.

T: (Write  $1\text{ m} = \underline{\hspace{1cm}}\text{ cm}$ .) How many centimeters are in 1 meter?

S: 100 centimeters.

Repeat process using the following possible sequence: 2 m, 3 m, 7 m, 4 m, 9 m.



#### A NOTE ON STANDARDS ALIGNMENT:

In this lesson and the entire module, students convert metric length units in the context of addition and subtraction problems involving mixed units. This lesson builds on the content of **2.MD.1** and **2.MD.5**.

On some occasions, students will work beyond the **4.MD.1** and **4.MD.2** standards by converting from a smaller to a larger unit. This conversion up will be established by creating a connection between units of measures related to place value.

If your students are not ready for the conversions up, you might work in small groups to further develop the number sense necessary for understanding these conversions and always accept answers in the smaller unit.

### Meter and Centimeter Number Bonds (8 minutes)

Materials: (S) Personal white boards

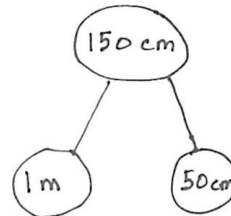
Note: This fluency prepares students to add and subtract meters and centimeters later in the lesson.

T: (Project a number bond with 150 centimeters written as the whole and 1 meter as one of the parts.) How many centimeters are in 1 meter?

S: 100 centimeters.

T: (Beneath 1 m, write 100 cm.) On your white boards, write a number bond filling in the missing part.

S: (Write a number bond with a whole of 150 cm and parts 1 m and 50 cm.)



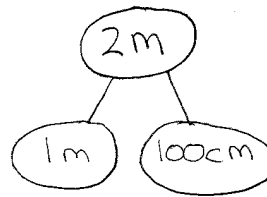
Repeat the process with wholes of 180 cm, 120 cm, 125 cm, 105 cm, and 107 cm.

T: (Project a number bond with 2 m written as the whole, 1 m as one of the parts, and \_\_\_\_ cm as the other part.) Fill in the missing part.

S: (Write a number bond with 2 m as the whole, 1 m as one of the parts, and 100 cm as the other part.)

T: Write the whole as an addition sentence with mixed units.

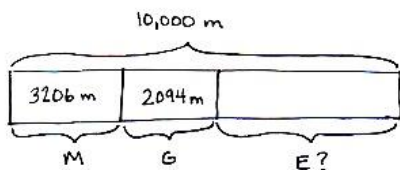
S: (Write  $1\text{ m} + 100\text{ cm} = 1\text{ m} + 1\text{ m} = 2\text{ m}$ .)



Repeat the process for  $2\text{ m} + 100\text{ cm} = 3\text{ m}$  and  $100\text{ cm} + 5\text{ m} = 6\text{ m}$ .

### Application Problem (8 minutes)

Martha, George, and Elizabeth sprinted a combined distance of 10,000 meters. Martha sprinted 3,206 meters. George sprinted 2,094 meters. How far did Elizabeth sprint? Solve using a simplifying strategy or an algorithm.



A

$$\begin{array}{r} 3206 \\ + 2094 \\ \hline 5300 \end{array} \quad \begin{array}{r} 10,000 \\ - 5,300 \\ \hline 4,700 \end{array}$$

B

$$\begin{array}{r} 3206 + 2094 = 5,300 \\ \begin{array}{r} 3,000 \quad 206 \\ 2,000 \quad 94 \end{array} \\ 10,000 - 5,300 = 4,700 \\ \begin{array}{r} 4,000 \\ \quad 700 \end{array} \end{array}$$

Elizabeth sprinted 4,700 meters.  
4 km 700 m

Note: This Application Problem builds on G4–M1–Lesson 19. Note that Solution A models the standard algorithm whereas Solution B records a simplifying strategy using number bonds, an application of strategies taught since Grade 1 in which students complete a unit or take from a whole unit. This Application Problem leads to the Concept Development of this lesson because the problem involves the metric unit of a meter.

**Concept Development (32 minutes)**

Materials: (T) Stapler and staples, ruler, meter stick, teacher-made poster with metric units (S) Personal white boards

**Introduction: Understanding 1 centimeter, 1 meter, and 1 kilometer in terms of concrete objects.**

Begin with a brief five-minute discussion of the length of a centimeter, meter, and **kilometer**.

- Use familiar, concrete examples such as a staple, the height of a countertop, and the distance to a local landmark that you know to be about 1 kilometer.
- Have students demonstrate the size of a centimeter and meter by indicating the size of the concrete examples that are given.
- Display a chart such as the one shown below.
- Add other examples to the chart, such as the width of a fingernail, the width of a door, the distance of two and a half laps around a running track, the length of a base ten cube, the height of a stack of five pennies, the outstretched arms of a child, and the distance around a soccer field four times. Show a meter stick to reference the exact size of a centimeter and a meter.

Metric Units of Length

| Centimeter       | meter                | kilometer                                     |
|------------------|----------------------|-----------------------------------------------|
| length of staple | height of countertop | distance from the school to the train station |



**NOTES ON MULTIPLE MEANS OF REPRESENTATION:**

Students who are English language learners may benefit from further discussion of concrete items that are about the same length as a centimeter, meter, and kilometer. Write examples on index cards of items that are a centimeter, a meter, or a kilometer in length. Have students place them in the appropriate columns of a chart. Provide students with blank index cards so they can create their own cards to add to the chart.



**NOTES ON MULTIPLE MEANS OF ENGAGEMENT:**

Ask students where they have heard the prefix *kilo-* before. As they learned in Grade 3, 1 kilogram equals 1,000 grams, so 1 kilometer equals 1,000 meters. Ask how many bytes are in 1 kilobyte.

**Problem 1**

Compare the sizes and note relationships between meters and kilometers as conversion equivalencies.

Use a two-column table as pictured on the right to support the following sequence.

| Distance |               |
|----------|---------------|
| km       | m             |
| 1        | 1,000         |
| 2        | <u>2,000</u>  |
| 3        | <u>3,000</u>  |
| 7        | <u>7,000</u>  |
| 70       | <u>70,000</u> |

T: 1 km = 1,000 m. How many meters are in 2 km? 3 km? 7 km? 70 km?

S: 2,000 m, 3,000 m, 7,000 m, 70,000 m.

T: Write 2,000 m = \_\_\_\_ km on your board. If 1,000 m = 1 km, 2,000 m = how many kilometers?

S: 2 kilometers.

Repeat for 8,000 m, 10,000 m, and 9,000 m.

T: Compare kilometers and meters.

**MP.7**

S: 1 kilometer is 1,000 times as much as 1 meter. → A kilometer is a longer distance because we need 1,000 meters to equal 1 kilometer.

T: (Display 1 km 500 m = \_\_\_\_\_ m.) Convert 1 km 500 m to meters. 1 kilometer is equal to how many meters?

S: 1,000 meters.

T: 1,000 meters plus 500 meters is 1,500 meters. (Fill in the blank.)

T: (Display 1 km 300 m = \_\_\_\_ m.) 1 kilometer 300 meters is equal to how many meters?

S: 1,300 meters.

Repeat with 5 km 30 m. (Anticipate the incorrect answer of 530 m.)

T: 2,500 meters is equal to how many kilometers?

S: 2 km 500 m. We made two groups of 1,000 meters, so we have 2 kilometers and 500 meters.

Repeat with 5,005 m.

**Problem 2**

Add **mixed units** of length using the algorithm or simplifying strategies.

Display horizontally 5 km + 2,500 m.

T: Talk for one minute with your partner about how to solve this problem.

S: We have 5 km and 2,500 m. → We can't add different units together. → We can rename the kilometers to meters before adding. 5 kilometers equals 5,000 meters, so 5,000 m + 2,500 m = 7,500 m. → I'm going to rename 7,500 m to 7 km 500 m.



**Problem 3**

Subtract mixed units of length using the algorithm or simplifying strategies.

- T: (Display horizontally: 10 km – 3 km 140 m.) Simplifying strategy or the algorithm? Discuss with a partner.
- S: Oh, for sure, I’m using the algorithm. There are no meters in the number I’m subtracting from. → That’s like 10 thousand minus 3 thousand 140. Algorithm for me. → I can do mental math. I’ll show you when we solve.
- T: Choose the way you want to do it. If you finish either before two minutes is up, try solving it a different way. Let’s have two pairs of students work at the board, one pair using the algorithm and one pair recording a mental math strategy.

After two minutes, review the student work on the board, which hopefully includes strategies such as those below. If not, gently supplement. Solutions A and B are algorithms. Solutions C, D, and E are simplifying strategies.

Ⓐ

$$\begin{array}{r} 10,000\text{ m} \\ - 3,140\text{ m} \\ \hline 6,860\text{ m} \end{array}$$

Ⓑ

$$\begin{array}{r} 9\text{ km } 1,000\text{ m} \\ - 3\text{ km } 140\text{ m} \\ \hline 6\text{ km } 860\text{ m} \end{array}$$

Ⓒ

$$\begin{array}{l} 10\text{ km} - 3\text{ km } 140\text{ m} \\ 10\text{ km} - 3\text{ km} = 7\text{ km} \\ 7\text{ km} - 140\text{ m} = 6\text{ km } 860\text{ m} \\ \hline 6\text{ km } 860\text{ m} \end{array}$$

Ⓓ

$860\text{ m} + 6\text{ km} = 6\text{ km } 860\text{ m}$   
 $860\text{ m} + 6,000\text{ m} = 6,860\text{ m}$

Ⓔ

$$3\text{ km } 140\text{ m} \xrightarrow{+860\text{ m}} 4\text{ km} \xrightarrow{+6\text{ km}} 10\text{ km}$$

$860\text{ m} + 6\text{ km} = 6\text{ km } 860\text{ m}$

- T: Look at Solution A. How did they set up for the algorithm?
- S: They rewrote everything as meters.
- T: What did they do in Solution B?
- S: They changed 1 kilometer for 1,000 meters right away.
- T: What happened in Solution C?
- S: They subtracted the 3 kilometers first.
- T: And then?
- S: Subtracted the meters from 1 kilometer after rewriting 1 kilometer as 1,000 meters
- T: Does anyone have a question for the mental math team?

**A NOTE ON STANDARDS ALIGNMENT:**

The concept of converting the answer into mixed units reaches beyond the fourth grade standard. For those students working above grade level, acknowledge the conversion. Students working at or below grade level are not expected to convert their answers.

- S: How did you know 1 thousand minus 140 was 860?
- S: We just subtracted a hundred and then thought of 40 less than 900. We know 6 tens and 4 tens is a hundred, so it wasn't too hard.
- T: What about Solution D?
- S: They used a number line to show a counting up strategy. It's like Solution E. They just represented it in a different way.
- T: And Solution E?
- S: They counted up from 3 km 140 m to 4 km first and then added 6 more km to get to 10 km.
- T: With your partner, take a moment to review the solution strategies on the board. Tell your partner why 6 km 860 m is equal to 6,860 m.
- S: The number line team showed it is because they matched kilometers to meters. → You can regroup 6 kilometers as 6,000 meters. → You can regroup 6,000 meters to 6 kilometers. → Both are the same amounts, but represented using different units, either mixed or a single unit.

**Problem 4**

Solve an application problem using mixed units of length using the algorithm or simplifying strategies.

Sam practiced his long jump in P.E. On his first attempt, he jumped 1 meter 47 centimeters. On his second attempt, he jumped 98 centimeters. How much farther did Sam jump on his first attempt than his second?

- T: Take two minutes with your partner to draw a tape diagram to model this problem. (Circulate as students work.)
- T: Your diagrams show a comparison between two values. How can you solve for the unknown?
- S: Subtract 98 cm from 1 m 47 cm.
- T: Will you use the algorithm or a simplifying strategy?

As before, invite two pairs to the board to solve as others work at their desks. Solution A shows the algorithm. Solutions B, C, and D show simplifying strategies.

1st  $1\text{ m } 47\text{ cm}$   
 2nd  $98\text{ cm}$  ?

A  $1\text{ m} = 100\text{ cm}$   
 $1\text{ m } 47\text{ cm} = 100\text{ cm} + 47\text{ cm}$   
 $\quad\quad\quad - 98\text{ cm}$   
 $\quad\quad\quad \hline$   
 $\quad\quad\quad 49\text{ cm}$

B  $1\text{ m } 47\text{ cm} - 98\text{ cm}$   
 $1\text{ m}$   
 $\downarrow$   
 $100\text{ cm} - 98\text{ cm} = 2\text{ cm}$   
 $47\text{ cm} + 2\text{ cm} = 49\text{ cm}$

C  $1\text{ m } 47\text{ cm} - 98\text{ cm} = 49\text{ cm}$   
 $\begin{array}{r} 100 \\ - 98 \\ \hline 2 \\ + 47 \\ \hline 49 \end{array}$

D  $98\text{ cm} \xrightarrow{+2} 1\text{ m} \xrightarrow{+47} 1\text{ m } 47\text{ cm}$

Sam jumped 49 cm farther on his first attempt.

### Problem Set (10 minutes)

Students should do their personal best to complete the Problem Set within the allotted 10 minutes. Some problems do not specify a method for solving. This is an intentional reduction of scaffolding that invokes MP.5, Use Appropriate Tools Strategically. Students should solve these problems using the RDW approach used for Application Problems.

For some classes, it may be appropriate to modify the assignment by specifying which problems students should work on first. With this option, let the careful sequencing of the Problem Set guide your selections so that problems continue to be scaffolded. Balance word problems with other problem types to ensure a range of practice. Assign incomplete problems for homework or at another time during the day.

### Student Debrief (10 minutes)

**Lesson Objective:** Express metric length measurements in terms of a smaller unit; model and solve addition and subtraction word problems involving metric length.

The Student Debrief is intended to invite reflection and active processing of the total lesson experience.

Invite students to review their solutions for the Problem Set. They should check work by comparing answers with a partner before going over answers as a class. Look for misconceptions or misunderstandings that can be addressed in the Debrief. Guide students in a conversation to debrief the Problem Set and process the lesson. You may choose to use any combination of the questions below to lead the discussion.

- What pattern did you notice in the equivalences for Problems 1 and 2 of the Problem Set? How did converting 1 kilometer to 1,000 meters in Problem 1(a) help you to solve Problem 2(a)?
- How did solving Problem 2 prepare you to solve Problem 3?

Name Jack Date \_\_\_\_\_

1. Find the equivalent measures.

|                            |                             |
|----------------------------|-----------------------------|
| a. 1 km = <u>1,000</u> m   | e. 1 m = <u>100</u> cm      |
| b. 4 km = <u>4,000</u> m   | f. 3 m = <u>300</u> cm      |
| c. 7 km = <u>7,000</u> m   | g. 80 m = <u>8,000</u> cm   |
| d. <u>18</u> km = 18,000 m | h. <u>120</u> m = 12,000 cm |

2. Find the equivalent measures.

|                                  |                                    |
|----------------------------------|------------------------------------|
| a. 3 km 312 m = <u>3,312</u> m   | d. 3 m 56 cm = <u>356</u> cm       |
| b. 13 km 27 m = <u>13,027</u> m  | e. 14 m 8 cm = <u>1408</u> cm      |
| c. 915 km 8 m = <u>915,008</u> m | f. 120 m 46 cm = <u>120,046</u> cm |

3. Solve.

a) 4 km - 280 m = 3,720 m

$$\begin{array}{r} 4 \text{ km} \\ 4,000 \text{ m} \\ - 280 \text{ m} \\ \hline 3,720 \text{ m} \end{array}$$

b) 1 m 15 cm - 34 cm = 81 cm

$$\begin{array}{r} 1 \text{ m} \\ 15 \text{ cm} \\ - 34 \text{ cm} \\ \hline 81 \text{ cm} \end{array}$$

c) Express your answer in the smaller of the two units:  
1 km 431 m + 13 km 169 m = 14,600 m

$$\begin{array}{r} 1,431 \text{ m} \\ + 13,169 \text{ m} \\ \hline 14,600 \end{array}$$

d) Express your answer in the smaller of the two units:  
231 m 31 cm - 14 m 48 cm = 21,683 cm

$$\begin{array}{r} 231 \text{ m} \\ 31 \text{ cm} \\ - 14 \text{ m} \\ 48 \text{ cm} \\ \hline 21,683 \text{ cm} \end{array}$$

e) 67 km 230 m + 11 km 879 m = 79 km 109 m

$$\begin{array}{r} 67 \text{ km} \\ 230 \text{ m} \\ + 11 \text{ km} \\ 879 \text{ m} \\ \hline 78 \text{ km} 1109 \text{ m} \\ 79 \text{ km} 109 \text{ m} \end{array}$$

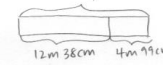
f) 67 km 230 m - 11 km 879 m = 55 km 351 m

$$\begin{array}{r} 67 \text{ km} \\ 230 \text{ m} \\ - 11 \text{ km} \\ 879 \text{ m} \\ \hline 56 \text{ km} 351 \text{ m} \\ 55 \text{ km} 351 \text{ m} \end{array}$$

COMMON CORE Lesson 1: Express metric measurement in a larger unit in terms of a smaller unit, reason about sizes of units, and model and solve addition and subtraction word problems involving metric units. 2.A.8  
Date: 5/10/13

Use a tape diagram to model each problem. Solve using mental math or an algorithm and write your answer as a statement.

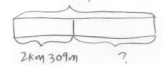
4. The length of Carter's driveway is 12m 38cm. His neighbor's driveway is 4m 99cm longer. How long is the neighbor's driveway?



$$\begin{array}{r} 12 \text{ m} 38 \text{ cm} \\ + 4 \text{ m} 99 \text{ cm} \\ \hline 16 \text{ m} 137 \text{ cm} \\ 1 \text{ m} 37 \text{ cm} \end{array}$$

The neighbor's driveway is 17m 37cm long.

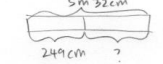
5. Enya walked 2km 309m from school to the store. Then she walked from the store to her home. If she walked a total of 5km, how far was it from the store to her home?



$$\begin{array}{r} 5 \text{ km} \\ 5,000 \text{ m} \\ - 2 \text{ km} 309 \text{ m} \\ \hline 2 \text{ km} 691 \text{ m} \end{array}$$

It is 2 km 691 m from the store to Enya's home.


6. Rachael has a rope 5m 32cm long that she cut into 2 pieces. One piece is 249cm long. How many centimeters long is the other piece of rope?



$$\begin{array}{r} 5 \text{ m} 32 \text{ cm} \\ 5,320 \text{ cm} \\ - 249 \text{ cm} \\ \hline 5,071 \text{ cm} \\ 283 \text{ cm} \end{array}$$

The other piece of rope is 283 cm long.

7. Jason rode his bike 529 fewer meters than Allison. Jason rode 1km 850m. How many meters did Allison ride?



$$\begin{array}{r} 1 \text{ km} 850 \text{ m} \\ + 529 \text{ m} \\ \hline 1 \text{ km} 1379 \text{ m} \\ 1 \text{ km} 379 \text{ m} \end{array}$$

Allison rode 2 km 379 meters.

COMMON CORE Lesson 1: Express metric measurement in a larger unit in terms of a smaller unit, reason about sizes of units, and model and solve addition and subtraction word problems involving metric units. 2.A.9

- For Problem 3, Parts (c) and (d), explain how you found your answer in terms of the smaller of the two units. What challenges did you face?
- When adding and subtracting **mixed units** of length, what are two ways that you can solve the problem? Explain to your partner.
- How did solving Problems 1, 2, and 3 help you to solve the rest of the problems in the Problem Set?
- Look at Problem 4 in the Concept Development. How did you draw your tape diagram? Explain to your partner how you solved this problem.
- What new math vocabulary did we use today to communicate precisely?
- How did the Application Problem connect to today's lesson?

### Exit Ticket (3 minutes)

After the Student Debrief, instruct students to complete the Exit Ticket. A review of their work will help you assess the students' understanding of the concepts that were presented in the lesson today and plan more effectively for future lessons. You may read the questions aloud to the students.

Name \_\_\_\_\_

Date \_\_\_\_\_

1. Find the equivalent measures.

a.  $1 \text{ km} = \underline{\hspace{2cm}} \text{ m}$

b.  $4 \text{ km} = \underline{\hspace{2cm}} \text{ m}$

c.  $7 \text{ km} = \underline{\hspace{2cm}} \text{ m}$

d.  $\underline{\hspace{2cm}} \text{ km} = 18,000 \text{ m}$

e.  $1 \text{ m} = \underline{\hspace{2cm}} \text{ cm}$

f.  $3 \text{ m} = \underline{\hspace{2cm}} \text{ cm}$

g.  $80 \text{ m} = \underline{\hspace{2cm}} \text{ cm}$

h.  $\underline{\hspace{2cm}} \text{ m} = 12,000 \text{ cm}$

2. Find the equivalent measures.

a.  $3 \text{ km } 312 \text{ m} = \underline{\hspace{2cm}} \text{ m}$

b.  $13 \text{ km } 27 \text{ m} = \underline{\hspace{2cm}} \text{ m}$

c.  $915 \text{ km } 8 \text{ m} = \underline{\hspace{2cm}} \text{ m}$

d.  $3 \text{ m } 56 \text{ cm} = \underline{\hspace{2cm}} \text{ cm}$

e.  $14 \text{ m } 8 \text{ cm} = \underline{\hspace{2cm}} \text{ cm}$

f.  $120 \text{ m } 46 \text{ cm} = \underline{\hspace{2cm}} \text{ cm}$

3. Solve.

a.  $4 \text{ km} - 280 \text{ m} =$

b.  $1 \text{ m } 15 \text{ cm} - 34 \text{ cm} =$

c. Express your answer in the smaller of the two units:

$1 \text{ km } 431 \text{ m} + 13 \text{ km } 169 \text{ m} =$

d. Express your answer in the smaller of the two units:

$231 \text{ m } 31 \text{ cm} - 14 \text{ m } 48 \text{ cm} =$

e.  $67 \text{ km } 230 \text{ m} + 11 \text{ km } 879 \text{ m} =$

f.  $67 \text{ km } 230 \text{ m} - 11 \text{ km } 879 \text{ m} =$



Name \_\_\_\_\_

Date \_\_\_\_\_

1.

| Distance |          |
|----------|----------|
| 71 km    | _____ m  |
| _____ km | 30,000 m |
| 81 m     | _____ cm |
| _____ m  | 400 cm   |

2.  $13 \text{ km } 20 \text{ m} = \underline{\hspace{2cm}} \text{ m}$ 3.  $401 \text{ km } 101 \text{ m} - 34 \text{ km } 153 \text{ m} = \underline{\hspace{2cm}}$ 

4. Gabe built a toy tower that measured 1 m 78 cm. After building some more, he measured it, and it was 82 cm taller. How tall is his tower now? Draw a tape diagram to model this problem. Use a simplifying strategy or an algorithm to solve and write your answer as a statement.

Name \_\_\_\_\_

Date \_\_\_\_\_

1. Find the equivalent measures.

a. 5 km = \_\_\_\_\_ m

b. 13 km = \_\_\_\_\_ m

c. \_\_\_\_\_ m = 17,000 m

d. 60 km = \_\_\_\_\_ m

e. 7 m = \_\_\_\_\_ cm

f. 19 m = \_\_\_\_\_ cm

g. \_\_\_\_\_ m = 2,400 cm

h. 90 m = \_\_\_\_\_ cm

2. Find the equivalent measures.

a. 7 km 123 m = \_\_\_\_\_ m

b. 22 km 22 m = \_\_\_\_\_ m

c. 875 km 4 m = \_\_\_\_\_ m

d. 7 m 45 cm = \_\_\_\_\_ cm

e. 67 m 7 cm = \_\_\_\_\_ cm

f. 204 m 89 cm = \_\_\_\_\_ cm

3. Solve.

a. 2 km 303 m – 556 m =

b. 2 m – 54 cm =

c. Express your answer in the smaller of the two units:

338 km 853 m + 62 km 71 m =

d. Express your answer in the smaller of the two units:

800 m 35 cm – 154 m 49 cm =

e. 701 km – 523 km 445 m =

f. 231 km 811 m + 485 km 829 m =

